

The curve C has equation $y=rac{1}{2}x^2+6$.

The line L has equation y=2x+m, where m is a positive constant.

(a) Sketch ${\cal C}$ and ${\cal L}$ on separate diagrams, showing the coordinates of the points at which ${\cal C}$ and ${\cal L}$ cut the axes.

(4 marks)

Given that line L is a tangent to C,

(b) find the value of m.

(5 marks)

(Total for question = 9 marks)



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Figure 1 shows a sketch of part of the curve with equation y=g(x). The curve has a maximum point A(-3,5), a minimum point B(4,-7), and passes through the origin O.

- (a) Sketch Figure 1 based on the given description of g(x). Clearly label the coordinates of A,B, and O.
- (3 marks)
- (b) On a new set of axes, sketch y=-2g(x). Clearly label the transformed coordinates of A,B, , and O.
- (3 marks)
- (c) On another set of axes, sketch y=g(x)+3. Clearly label the transformed coordinates of $A,B,\$ and O.
- (3 marks)

(Total for question = 9 marks)



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eClassroom

Figure 1 shows a sketch of the curve with equation y = h(x), where

$$h(x) = (x+3)^2(x-4).$$

The curve **touches** the x-axis at (-3,0), **crosses** the x-axis at (4,0), and **crosses** the y-axis at (0,-36).

(a) Sketch Figure 1 based on the given description of h(x). Clearly label all intercepts and the turning point at (-3,0).

(3 marks)

(b) Write down the equation of the curve y=h(x-2).

(1 mark)

(c) Sketch the curve y=h(x-2). Clearly label all intercepts.

(3 marks)

(Total for question = 7 marks)



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The curve C passes through the point (-2,0), touches the x-axis at the point (3,0), and has a maximum at (0,6).

- (a) Sketch Figure 1 based on this description of ${\cal C}$. Clearly label all intercepts and the turning points.
- (4 marks)
- (b) The equation of ${\cal C}$ is of the form:

$$y = x^3 + px^2 + qx + r.$$

Use the given points to find the values of p,q, and r.

(4 marks)

(Total for question = 8 marks)

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The curve C has equation $y=\frac{2}{x+1}$, $x \neq -1$. The curve crosses the y-axis at A .

- (a) Sketch Figure 1 showing the graph of ${\cal C}$. Clearly label any asymptotes and the coordinate of ${\cal A}$. (3 marks)
- (b) The curve D has equation $y=x(x-3)^2$. Sketch Figure 1 for D, and label all intercepts. (3 marks)
- (c) Using your sketches, state the number of real solutions to the equation

$$x(x-3)^2 = \frac{2}{x+1}.$$

(1 mark)

(Total for question = 7 marks)



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- (a) On separate axes, sketch Figure 1 for the following:
- (i) y=-2x+b, where b is a positive constant.

(ii)
$$y=rac{4}{x}-2$$
.

In each case, clearly label any asymptotes and the point where the graph crosses the y-axis (if it exists). (4 marks)

(b) Given that y=-2x+b, where b is a positive constant, meets $y=\frac{4}{x}-2$ at two distinct points, show that

$$(b+2)^2 > 32.$$

(3	mar	ks)
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